

## a031curnt[001-004]: Following, Opposing and Slanting current

### Purpose

The purpose of these tests is to validate wave propagation in the presence of currents (current-induced refraction and shoaling).

### Situation

A deep water region of constant depth, 4000 m long and infinitely wide is considered (essentially a one-dimensional situation; Figure 1). For all cases monochromatic, uni-directional waves propagate in positive x-direction. The up-wave boundary is at  $x = 0$ . The incident wave height  $H_i$  and period  $T_i$  are 1 m and 10 s respectively.

For cases a031curnt001 and a031curnt002 the wave direction is parallel to the x-axis. For case a031curnt001 the current direction is in positive x-direction. The current velocity increases linearly from 0 to 2 m/s (as in Figure 11, following current and Figure 2, opposing current). For case a031curnt002 the current direction is in negative x-direction (opposing current) and increases linearly from 0 to -2 m/s in positive x-direction.

For case a031curnt003 the wave direction at the up-wave boundary is  $120^\circ$ . For a031curnt004 the wave direction at the up-wave boundary is  $60^\circ$ . For these cases the current is parallel to the x-axis and in positive x-direction (as in Figure 1). The current velocity increases linearly from 0 to 2 m/s in positive x-direction.

For all four cases wind is absent. The water is infinitely deep.

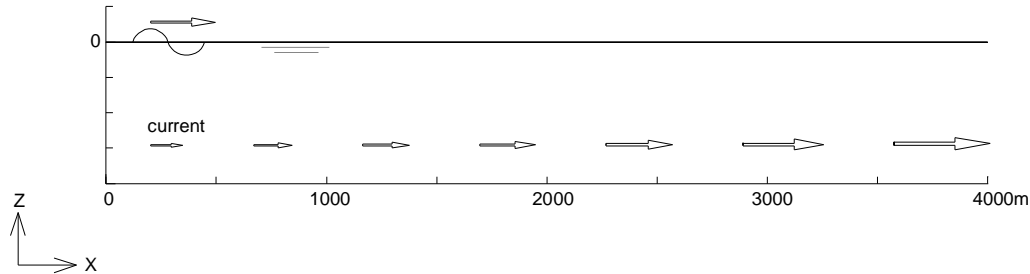


Figure 1 Following current condition

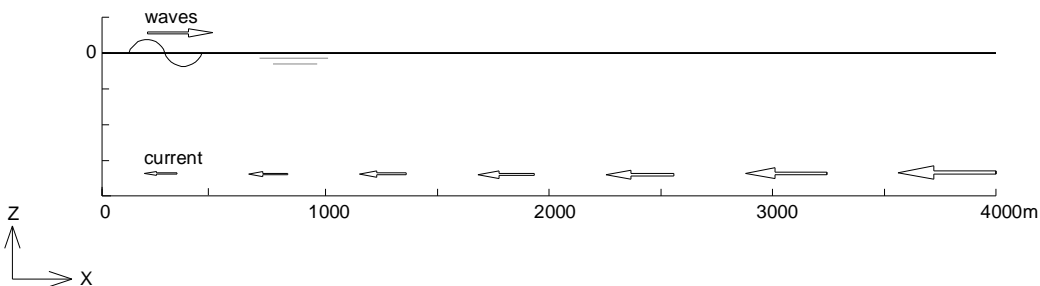


Figure 2 Opposing current condition

### Comparison

Model results for the following current and the opposing current cases are compared with an analytical solution. The analytical solution is calculated with (Phillips, 1977; Jonsson, 1993):

## a031curnt Following, opposing and slanting current

$$\frac{H^2}{H_i^2} = \frac{c_i^2}{c(c+2U)} \quad \text{where} \quad \frac{c}{c_i} = \frac{1}{2} + \frac{1}{2} \left( 1 + 4 \frac{U}{c_i} \right)^{\frac{1}{2}} \quad (\text{A3.1})$$

For the slanting current cases, the analytical solutions for the wave direction and the wave height, using Snell's law:  $\sin \theta / c = \text{constant}$ , are (see e.g., Hedges, 1987; Jonsson, 1993):

$$\begin{cases} \theta = \arccos \left( \frac{gk_i \cos(\theta_i)}{[\omega - Uk_i \cos(\theta_i)]^2} \right) \\ H = H_i \sqrt{\frac{\sin(2\theta_i)}{\sin(2\theta)}} \end{cases} \quad (\text{A3.2})$$

Comparison is made for wave height, wave period and wave direction.

## Default model commands

COMPUTATIONAL GRID											
1D/2D		XPC		YPC		ALPC		XLENC		YLENC	
2D		0		0		0		16000		4000	
	AX	AY	DIR1	DIR2	$\Delta\theta$	FLOW	FHIGH	MSC			
001	400	40	30°	150°	2°	0.05	0.25	40			
002	400	40	30°	150°	2°	0.05	0.25	40			
003	640	40	60°	140°	1°	0.05	0.25	40			
004	640	40	10°	70°	1°	0.05	0.25	40			
PHYSICS											
	GEN	BREAK	FRIC	TRIADS	QUAD	WCAP	REFRAC	FSHIFT	SETUP		
	off	off	off	off	off	on	on	on	off		
BOUNDARY CONDITIONS											
	TYPE	BOU	C/V	P/R	SHAPE	PE/ME	DSPR	HS	PER	PDIR	DD
001	side	S	con	par	Gauss 0.01	peak	power	1	10	90°	500
002	side	S	con	par	Gauss 0.01	peak	power	1	10	90°	500
003	side	S	con	par	Gauss 0.01	peak	power	1	10	120°	500
004	side	S	con	par	Gauss 0.01	peak	power	1	10	60°	500
BOTTOM:			WIND:			CURRENT:			WATER LEVEL:		
001	'a031curnt001.bot'		-			'a031curnt001.cur'			-		
002	'a031curnt002.bot'		-			'a031curnt002.cur'			-		
003	'a031curnt003.bot'		-			'a031curnt003.cur'			-		
004	'a031curnt004.bot'		-			'a031curnt004.cur'			-		

## References

- Phillips, O.M, 1977: The dynamics of the upper ocean, 2<sup>nd</sup> edition, Cambridge University Press, 336 p.
- Jonsson, I.G., 1993: *The Sea*, Ocean Engineering Science, 9, Part A
- Hedges, T.S., 1987: Combination of waves and currents: an introduction, *Proc. Instn. Civ. Engrs.*, Part 1, 82,567-585

## Acknowledgements